



Listen as your teacher explains how the model of the nomograph works. Then open the **NOMOGRPH** program on your calculator and work with a partner to complete the activity.



### Problem 1 – “What’s my Rule?”

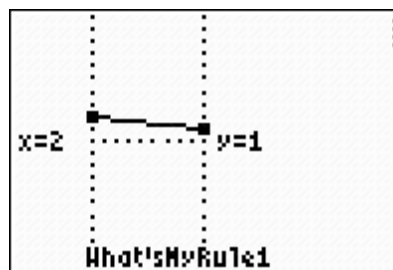
Select **1:What’sMyRule** and then choose **1:What’sMyRule1**.

Enter a value of  $x$ . The nomograph relates it to a  $y$ -value by substituting the value of  $x$  into the function’s rule.

Find the “mystery rule” for  $f(x)$  that pairs each value for  $x$  with a value for  $f(x)$ .

$f(x) =$  \_\_\_\_\_

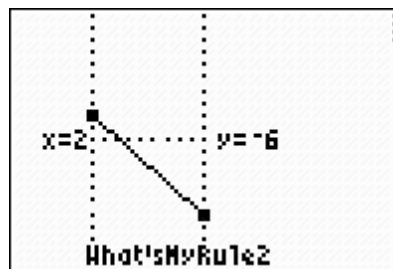
When you are finished, enter the value **86** to return to the menu.



### Problem 2 – A more difficult “What’s my Rule?”

The second nomograph (**1:What’sMyRule > 2:What’sMyRule2**) follows a non-linear function rule. As before, enter values for  $x$  and find the rule for this new function  $f(x)$ . Test your rule using the nomograph.

$f(x) =$  \_\_\_\_\_



### Problem 3 – The “What’s my Rule?” Challenge

The rule challenge is to make up a new rule (of the form  $ax + b$  or  $ax^2 + b$ ) for  $f(x)$ , and have a partner guess your rule by using the nomograph.

Choose **1:What’sMyRule > 3:RuleChallenge** from the menu. When prompted, enter an expression to complete the function and press **ENTER**. Then, exchange graphing calculators with your partner, who will use the nomograph to discover your rule. Then, repeat.

In this round,  
you create a  
function that  
your partner  
tries to guess.  
Enter a  
function:  
 $f(x)=x$

List at least four of the functions you and your partner explored with the nomograph.

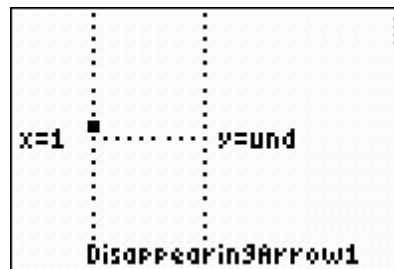
$f(x) =$  \_\_\_\_\_       $f(x) =$  \_\_\_\_\_       $f(x) =$  \_\_\_\_\_       $f(x) =$  \_\_\_\_\_

**Problem 4 – The case of the disappearing arrow**

Return to the program's main menu and choose **2:DisappearArrow > 1:Disappear1** to show a nomograph for the function  $f(x) = \sqrt{x^2 - 4}$ . Enter values for  $x$ . Observe what happens as the value of  $x$  changes.

When does the arrow disappear? \_\_\_\_\_

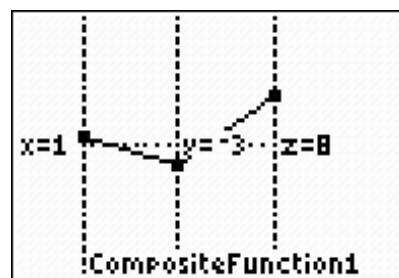
Why does the arrow disappear? \_\_\_\_\_



**Problem 5 – Composite functions: “wired in series”**

Choose **3:CompositeFunc > 1:CompositeFunc1** and enter a value for  $x$ .

This nomograph consists of three vertical number lines and behaves like *two* function machines wired in series. The point at  $x$  identifies a domain value on the first number line and is dynamically linked by the function  $f_1(x) = 3x - 6$  to a range value  $y$  on the middle number line. That value is then linked by a second function  $f_2(x) = -2x + 2$  to a value  $z$  on the far right number line.



Either of the two notations  $f_2(f_1(x))$  or  $f_2 \circ f_1$  can be used to describe the **composite function** that gives the result of applying function  $f_1$  *first*, and then applying function  $f_2$  to that result.

For example, the number 4 is linked to 6 by  $f_1$  (because  $f_1(4) = 6$ ), which in turn is linked to  $-10$  by  $f_2$  (because  $f_2(6) = -10$ ). Set  $x = 4$  and confirm that  $y = 6$  and  $z = -10$ .

Find a rule for the single function  $f_3$  that gives the same result as  $f_2(f_1(x))$  for all values of  $x$ . To test your answer, return to the **3:RuleChallenge** (What's My Rule) and define  $f_3$  to be your function.

$$f_3(x) = \underline{\hspace{2cm}}$$

Now compute several values, for each function, such as  $f_2(f_1(4))$  and  $f_3(4)$ . Are they equal?

Compute and compare the following.

$$f_2(f_1(3)) = \underline{\hspace{2cm}}$$

$$f_1(f_2(3)) = \underline{\hspace{2cm}}$$

Try other values of  $x$ . Does the order in which you apply the functions matter?

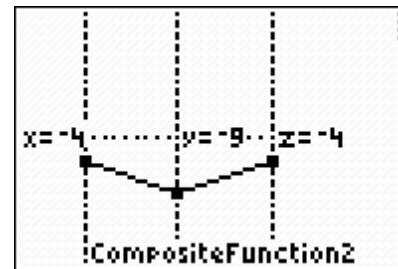
Test your understanding by completing another example:

In **3:CompositeFunc > 3:MakeYourOwn**,  $f_1(x) = (x - 1)^2$  and  $f_2(x) = 2x + 3$ . Find a rule for both  $f_2 \circ f_1$ . Then switch the order of the functions and find a rule for  $f_1 \circ f_2$ . Test your answer by computing several values for each function.

$f_2(f_1(x)) =$  \_\_\_\_\_       $f_1(f_2(x)) =$  \_\_\_\_\_

**Problem 6 – A well-behaved composite function**

Some composite functions are more predictable than others. The nomograph in **2:CompositeFunc2** shows the function  $f_1(x) = 3x + 3$  composed with a mystery function  $f_2$ . Grab and drag the base of the arrow at  $x$ .



What do you notice about the composite function  $f_2 \circ f_1$ ?

Play “What’s my Rule?” to find the rule for  $f_2$ .

$f_2(x) =$  \_\_\_\_\_

Use **3:MakeYourOwn** to compute and compare the following.

$f_2(f_1(3)) =$  \_\_\_\_\_       $f_1(f_2(3)) =$  \_\_\_\_\_

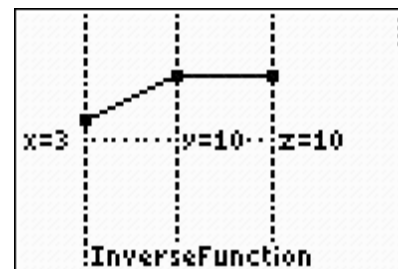
Try other values of  $x$ . Does the order in which you apply the functions matter?

**Problem 7 – Inverse functions**

The “inverse” of a function  $f$ , denoted  $f^{-1}$ , “undoes” the function—it maps a point  $y$  from the range back to its original  $x$  from the domain. You can think of a function and its inverse as a special case of function composition. (This is what was shown in Problem 6.)

By definition,  $f_2$  is the inverse of  $f_1$ , if and only if:

- $f_2(f_1(x)) = x$  for every  $x$  in the domain of  $f_1$ , and
- $f_1(f_2(x)) = x$  for every  $x$  in the domain of  $f_2$ .



In the context of the nomograph,  $f_2$  is the inverse of  $f_1$  if  $f_2(f_1(x))$  horizontally aligns with  $x$  for all values in the domain of  $f_1$  (i.e.  $z = x$ ), and vice versa.



# Advanced Algebra Nomograph

The nomograph in **4:InverseFunc > 1:InverseFunc**.

shows the composite function  $f_2 \circ f_1$ , where  $f_1(x) = 2x + 4$  and  $f_2(x) = x$ . See if you can figure out what the rule for  $f_2(x) =$  \_\_\_\_\_  $f_2$  must be in order for  $f_1$  and  $f_2$  to be inverse functions.

When prompted, enter an expression to complete the function and an x-value to test your answer.

## Problem 8 – Disappearing arrows in a composite function

The nomograph in **2:DisappearArrow > 2:Disappear2** shows the composite function  $f_2 \circ f_1$  where  $f_1(x) = 2x - 6$  and  $f_2(x) = \sqrt{x}$ . Try several values of x. Watch as one of the arrows disappears.

Which arrow disappears? \_\_\_\_\_

When and why does it disappear? \_\_\_\_\_

## Problem 9 – “Almost” inverses and more missing arrows

The nomograph in **4:InverseFunc > 2:AlmostInverse1** shows the composite function  $f_2 \circ f_1$  where  $f_1(x) = \sqrt{x}$  and  $f_2(x) = x^2$ . Enter several values for x.

When does  $f_2$  act like the inverse of  $f_1$ ? \_\_\_\_\_

When does  $f_2$  NOT act like the inverse of  $f_1$ ? \_\_\_\_\_

When and which arrow(s) disappears? \_\_\_\_\_

The nomograph is **4:InverseFunc > 3:AlmostInverse2** reverse the definitions, that is, defines  $f_1(x) = x^2$  and  $f_2(x) = \sqrt{x}$ .

Test some values for x in the nomograph.

When does  $f_2$  act like the inverse of  $f_1$ ? \_\_\_\_\_

When does  $f_2$  NOT act like the inverse of  $f_1$ ? \_\_\_\_\_

When and which arrow(s) disappears? \_\_\_\_\_